



SOLVING EQUATIONS WITH VARIABLES ON BOTH SIDES

**LO: To solve equations
involving complex equations.**

25 September 2025

Week 5, Day 4

25/09/2025

Solving Equations with variables on both sides

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Key words: Transpose, isolate, combine, like terms, multi-step

Mental Maths



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MENTAL MATHS: Solve for the unknown.

$$1) \ c - 1 = 4$$

$$2) \ 8 = c + c$$

$$3) \ -2x = -4$$

$$4) \ 3c + 4c = 7$$

$$5) \ 6 = -3c$$

$$6) \ 5y = 1 - 4$$

$$7) \ y - 3 = 9$$

$$8) \ c + 2 = 10$$

$$9) \ -2x = 10$$

$$10) \ 88v = -11$$



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MENTAL MATHS (ANSWERS)

Solve for the unknown.

C = 5

1) $c - 1 = 4$

C = 4

2) $8 = c + c$

X = 2

3) $-2x = -4$

C = 1

4) $3c + 4c = 7$

C = -2

5) $6 = -3c$

6) $5y = 1 - 4$ **C = -3/5**

7) $y - 3 = 9$ **C = 12**

8) $c + 2 = 10$ **C = 8**

9) $-2x = 10$ **C = -5**

10) $88v = -11$ **C = -1/8**



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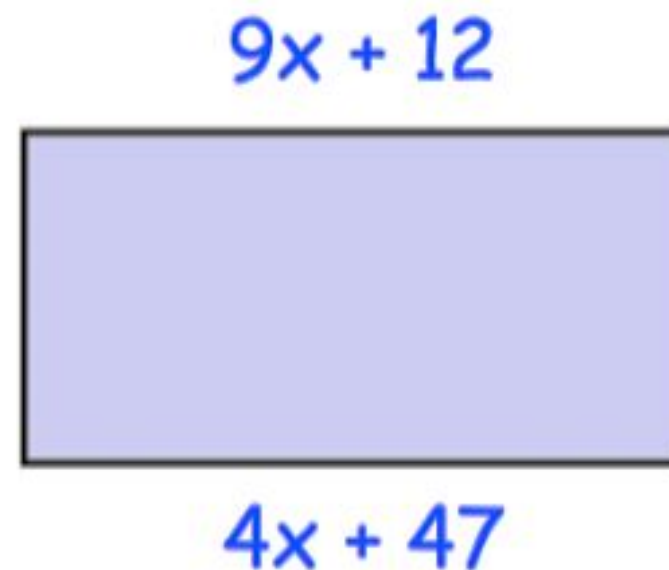
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STARTER

Shown is a rectangle

(a) Explain why $9x + 12 = 4x + 47$

(b) Find x





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STARTER (ANSWERS)


- (a) The opposite sides of a rectangle have the same length
- (b) $x = 7$



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GCSE/iGCSE Assessment Objective Specification – Foundation/Higher

 **A** understand that symbols may be used to represent numbers in equations or variables in expressions and formulae

A solve linear equations, with integer or fractional coefficients, in one unknown in which the unknown appears on either side or both sides of the equation

B set up simple linear equations from given data

The three angles of a triangle are a° , $(a + 10)^\circ$, $(a + 20)^\circ$.
Find the value of a



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KEY CONCEPT:

Example:

1) Solve for z : $7z - (3z - 4) = 12$

Solution:

Step 1. Simplify the left side of the equation by removing parentheses and combining like terms.

Distribute through by -1 .

$$7z - 3z + 4 = 12$$

Combine like terms on the left side of the equation.

$$4z + 4 = 12$$

Step 2. Use subtraction to isolate the variable term on the left side of the equation.

Subtract 4 from each side of the equation.

$$4z + 4 - 4 = 12 - 4$$

$$4z = 8$$

Step 3. Use division to solve for the variable.

Divide each side of the equation by 4.

The solution to $7z - (3z - 4) = 12$ is $z = 2$.



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My Turn

Solve the following equations:

(a) $7x + 9 = 2x + 19$

$$\begin{array}{rcl} & \boxed{-2x} & \boxed{-2x} \\ 7x + 9 & = & 2x + 19 \\ 5x + 9 & = & 19 \\ & \boxed{-9} & \boxed{-9} \\ 5x & = & 10 \\ \boxed{\div 5} & & \boxed{\div 5} \\ x & = & 2 \end{array}$$

Your Turn

(b) $3x - 1 = 6 - 4x$

$$\begin{array}{rcl} & \boxed{+4x} & \boxed{+4x} \\ 3x - 1 & = & 6 - 4x \\ 7x - 1 & = & 6 \\ & \boxed{+1} & \boxed{+1} \\ 7x & = & 7 \\ \boxed{\div 7} & & \boxed{\div 7} \\ x & = & 1 \end{array}$$



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MINI PLENARY:

Solve: $5x + 7 = 4x + 2$

The answer is $x = 5$

TRUE

Stand Up

FALSE

Remain Seated



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MINI PLENARY:

Solve: $9x - 5 = -2x + 50$

The answer is $x = 5$

TRUE

Stand Up

FALSE

Remain Seated



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MINI PLENARY:

Solve: $4x + 5 = 2x + 3$

The answer is $x = -1$

TRUE

Stand Up

FALSE

Remain Seated



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Worked example

Solve the equation $4(2a - 1) = 32 - 3(2a - 2)$.

$$4(2a - 1) = 32 - 3(2a - 2)$$

$$8a - 4 = 32 - 6a + 6$$

Multiply out the brackets. Take care with the minus signs.

$$8a - 4 = 38 - 6a$$

Collect like terms on the right-hand side. $32 + 6 = 38$

$$8a + 6a = 38 + 4$$

Rearrange to get like terms on both sides.

$$14a = 42$$

$$a = \frac{42}{14} = 3$$

Simplify and then solve.



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Core Task 1:

1. $8x + 8 = 2x + 62$

2. $7x + 3 = x + 33$

3. $6x + 5 = 3x + 17$

4. $7x + 7 = 3x + 7$

5. $7x + 10 = 4x + 25$

6. $7x + 4 = 2x + 29$

7. $5x + 10 = 4x + 14$

8. $8x + 1 = 4x + 29$

Core Task 2:

1. $8 - 3x = 20 - 6x$

2. $8 - 4x = -10x - 28$

3. $8 - 3x = 5x + 64$

4. $5x + 1 = 49 - 3x$

5. $7 - 9x = 15 - 10x$

6. $4 - 5x = 32 - 9x$

7. $10x + 6 = 42 - 2x$

8. $3 - 5x = 3x + 11$



Core Task

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1. $10(x - 8) = 3x - 66$

2. $5(x + 4) = 9x - 12$

Task 3:

3. $7(x + 5) = 10x + 20$

4. $7(x - 2) = 9x - 16$

7. $3(x - 10) = 2x - 25$

8. $10(x + 6) = 3x + 60$

9. $3(x - 4) = 4x - 18$

10. $5(x - 8) = 10x - 45$

5. $6(x + 3) = 10x - 18$

6. $9(x + 2) = 4x + 23$



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Extension

Solve the equations.

1 a. $-4(-4 - x) = \frac{7x}{-8}$

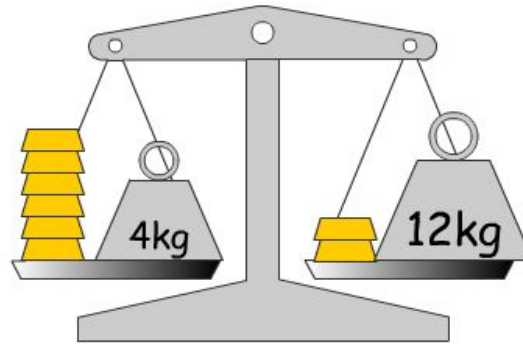
1 b. $\frac{-3c}{5} = 5 - 4c$



Plenary

LO: To solve equations involving complex equations.

05:00



What is the weight of one bar of gold in the picture?

Write the picture as an equation and solve it.

$$6x + 4 = 2x + 12$$

$$\begin{array}{rcl} & \boxed{-2x} & \boxed{-2x} \\ 4x + 4 & = & 12 \\ & \boxed{-4} & \boxed{-4} \\ 4x & = & 8 \\ \boxed{\div 4} & & \boxed{\div 4} \\ x & = & 2 \end{array}$$

How do you feel?
S-Secure
M-Met
W-Working
towards